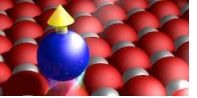




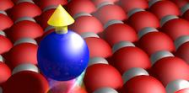
En raison du festival Balélec, nous avons dû procéder au(x) changement(s) de salle suivant pour votre cours :

Matière	Enseignant	Classe	Date	Heure	Salles concernées	Nouvelle salles
PHYS-510	<u>Pivetta</u> /Rusponi	PH-MA2	08.05.2025	8h-12h	CM 1 221	PH H3 31



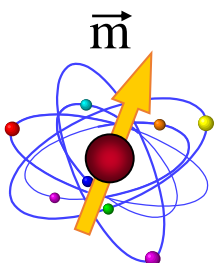
Lecture 7

Spin Orbit Torque (SOT)

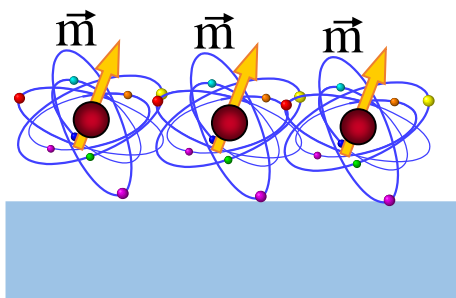
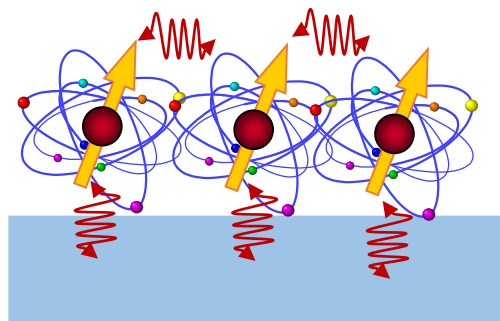


The spintronics “goose game”

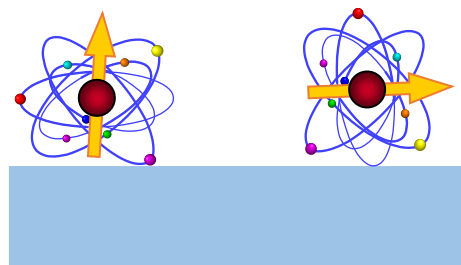
Atom magnetism



interactions between spins and with the supporting substrate

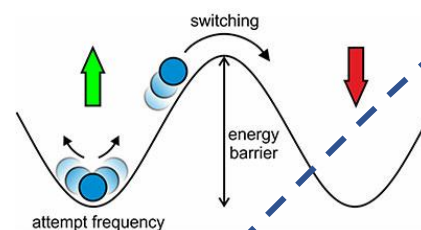
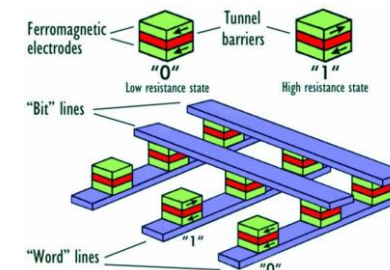
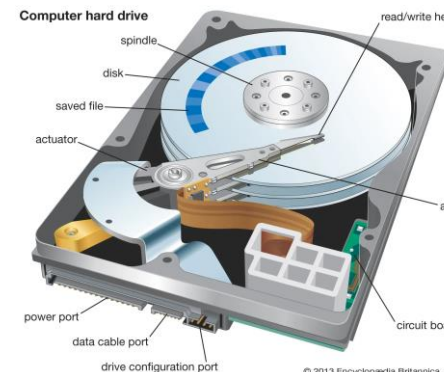


magnetic moment in a cluster and/or on a support

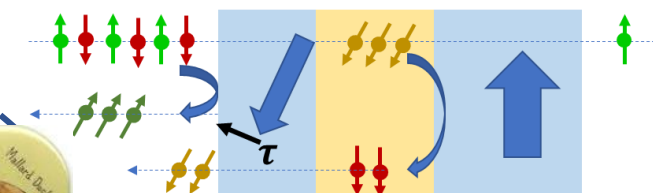


Magnetization easy axis

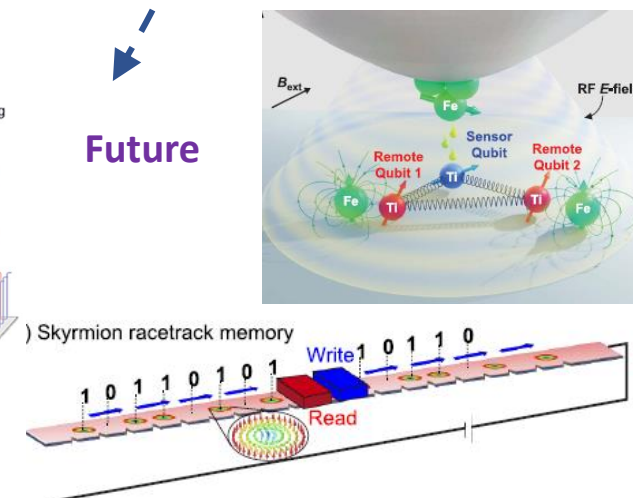
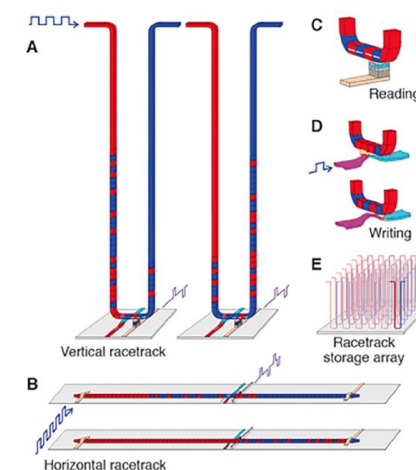
applications

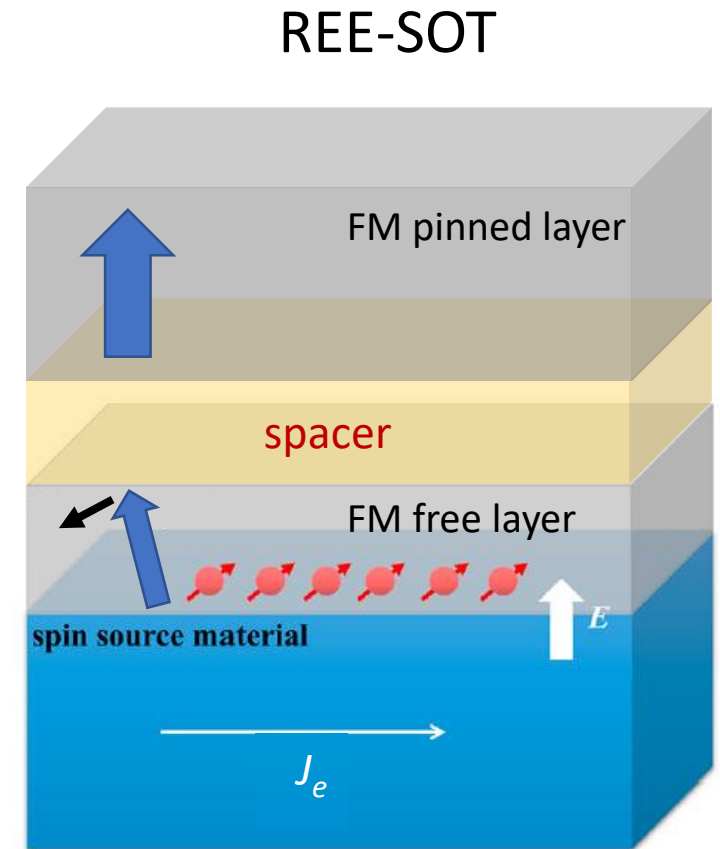
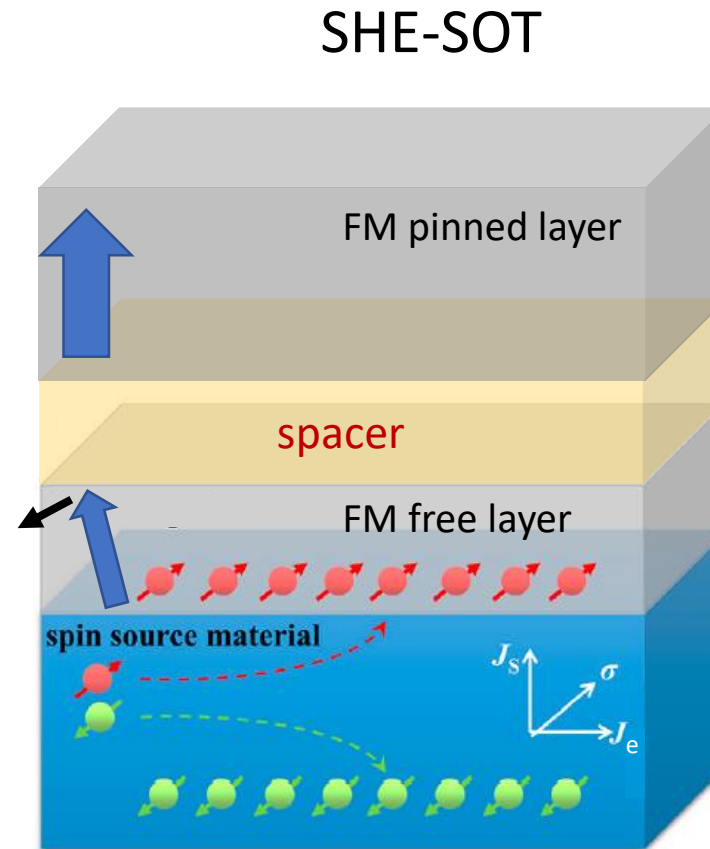
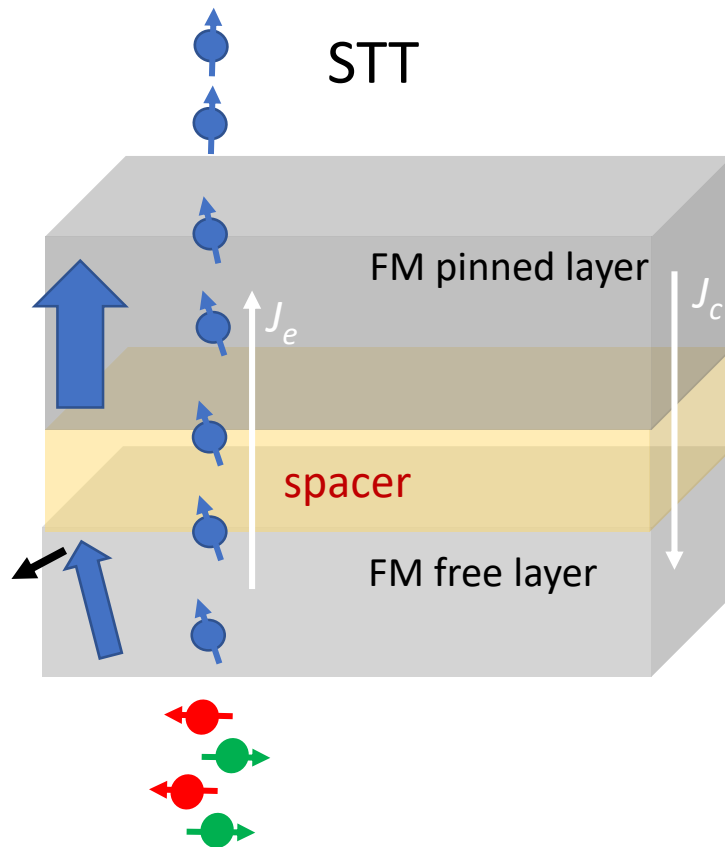


STT - SOT



Future





SOT employs in-plane current injection to write:

- 1) separates the reading and writing paths
- 2) Less power required since current does not need to pass through the insulating spacer



A free electron with spin σ and moment \mathbf{p} moving in an external magnetic field \mathbf{B} feels:



$$F_{Lorentz} = \frac{-e}{m} \mathbf{p} \times \mathbf{B}$$

$$H_{Zeeman} = -\mu_B \mathbf{B} \cdot \sigma$$

In crystals, electrons move with relativistic speed in the gradient of the crystal field potential. In the electron rest frame, this correspond to a magnetic field:



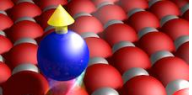
$$\mathbf{B}_{eff} = \frac{1}{mc^2} \nabla V \times \mathbf{p}$$

Spin-orbit coupling:

$$H_{SO} = -\mu_B \mathbf{B}_{eff} \cdot \sigma = -\mu_B/mc^2 (\nabla V \times \mathbf{p}) \cdot \sigma \propto \mathbf{l} \cdot \sigma$$

A twofold degenerate spin level might be split by SOC into two levels with spin parallel ($H_{SO} \propto \mathbf{l} \cdot \sigma$) and antiparallel ($H_{SO} \propto -\mathbf{l} \cdot \sigma$) to the orbit.

However, such splitting is symmetry forbidden for central symmetric systems (impossible to define the direction for spin up and down).



Rashba-Edelstein effect (REE): 2D interfaces

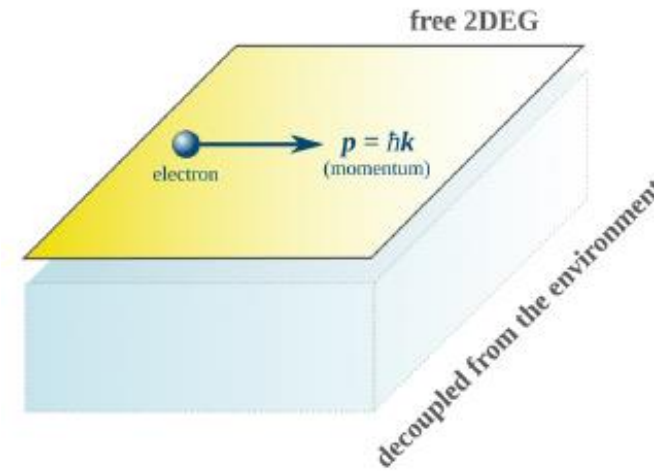
The absence of an inversion symmetry center at the crystal surface or at 2D interfaces breaks this symmetry

Free-standing 2D electron gas: $V = V_{at}$
Symmetric case

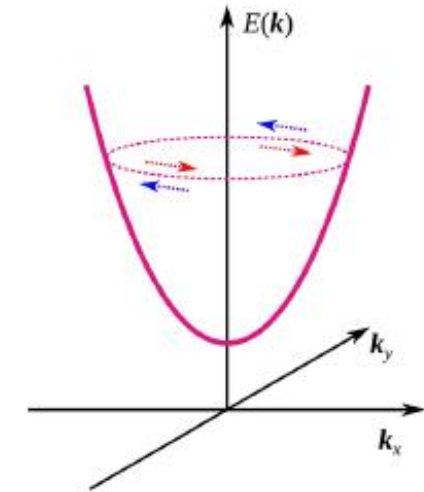
$$H = \frac{p^2}{2m_e} + eV_{at} - \frac{e\hbar}{2m_e^2 c^2} (\nabla V_{at} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma}$$

N.B.:

- 1) in these Hamiltonians V_{ee} is not included for simplicity
- 2) at surface electrons move parallel to the surface $\rightarrow \mathbf{p} = \mathbf{p}_{//}$



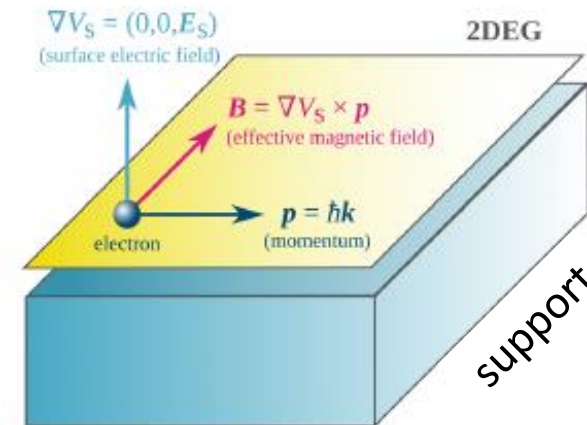
(c)



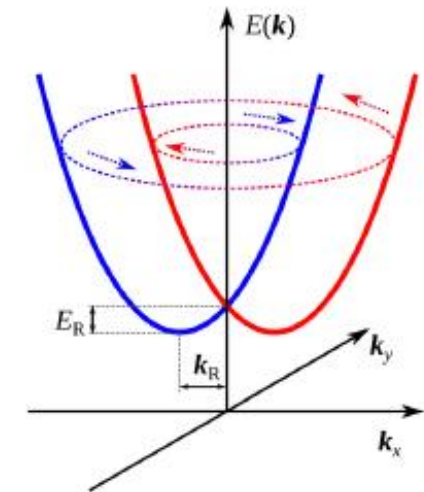
(d)

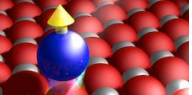
2D electron gas + support: $V = V_{at} + E_s z$
Broken symmetry

$$H = \frac{p^2}{2m_e} + eV_{at} - \frac{e\hbar}{2m_e^2 c^2} (\nabla V_{at} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma} + \frac{e\hbar E_s}{2m_e^2 c^2} (\hat{\mathbf{z}} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma}_{//} + eE_s z$$

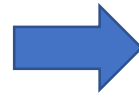


E_s originates from the atomic potential perturbed by the breaking symmetry at interface





$$H = \frac{\mathbf{p}^2}{2m_e} + eV_{at} - \frac{e\hbar}{2m_e^2c^2} (\nabla V_{at} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma} + \\ - \frac{e\hbar E_s}{2m_e^2c^2} (\hat{\mathbf{z}} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma}_{//} + eE_s z$$



$$H = \frac{\mathbf{p}^2}{2m_e} + eV + V_{SO} \mathbf{l} \cdot \boldsymbol{\sigma} + \\ H_{RE} + eE_s z$$

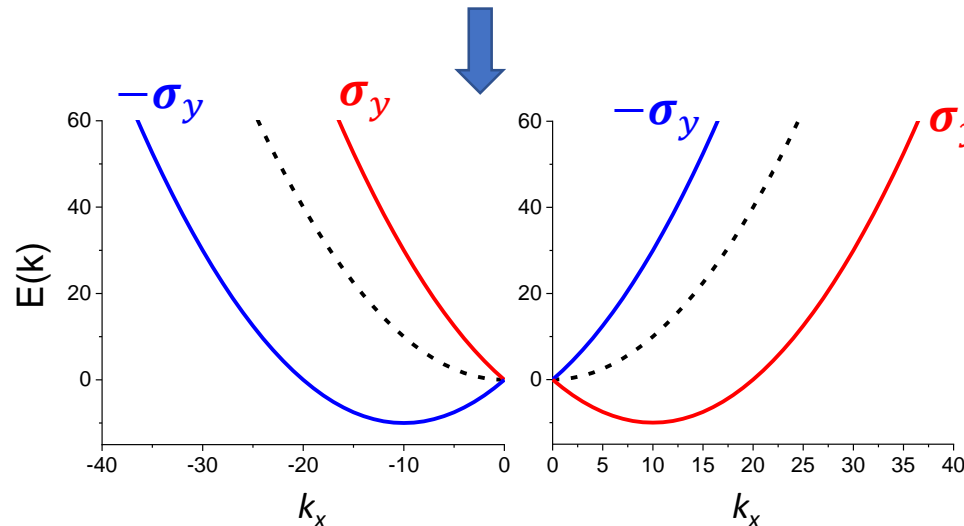
RE (Rashba-Edelstein) Hamiltonian:

$$H_{RE} = \frac{-e\hbar E_s}{2m_e^2c^2} (\hat{\mathbf{z}} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma}_{//} = \frac{-e\hbar^2 E_s}{2m_e^2c^2} (\hat{\mathbf{z}} \wedge \mathbf{k}_{//}) \cdot \boldsymbol{\sigma}_{//} = \alpha_{RE} (\hat{\mathbf{z}} \wedge \mathbf{k}_{//}) \cdot \boldsymbol{\sigma}_{//}$$

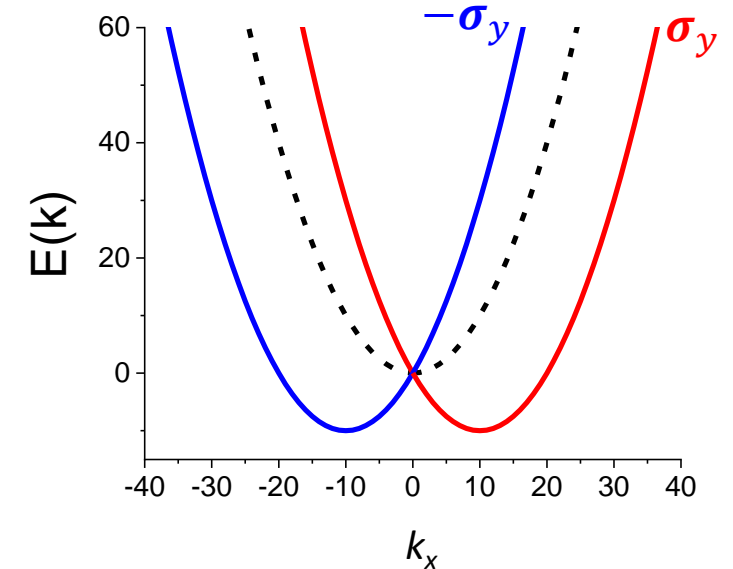
Because of SOC:

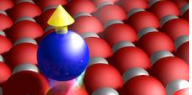
- 1) spins align perpendicularly to the momenta
- 2) splitting of spin bands

Inverted splitting between spin polarized bands at inverted wave vector \mathbf{k} (black corresponds to $H_{RE} = 0$)



1D case



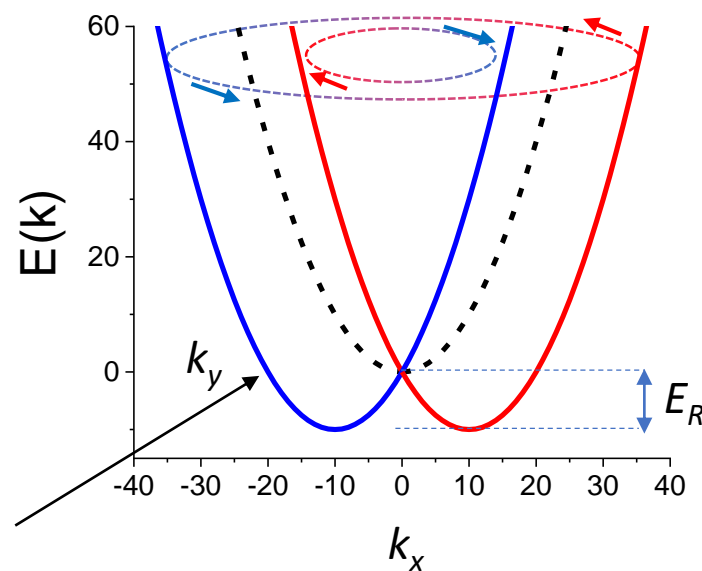
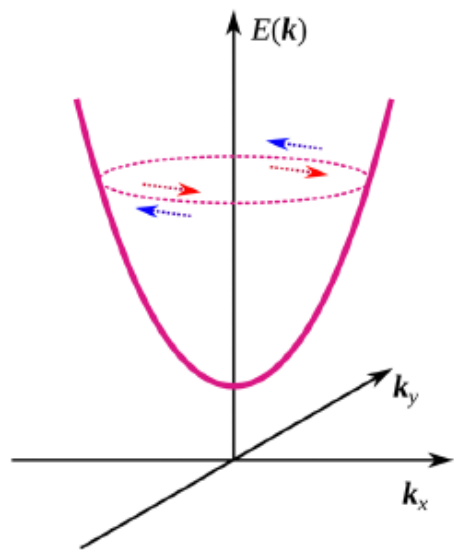


Because of SOC:

- 1) spins align perpendicularly to the momenta
- 2) splitting of spin bands

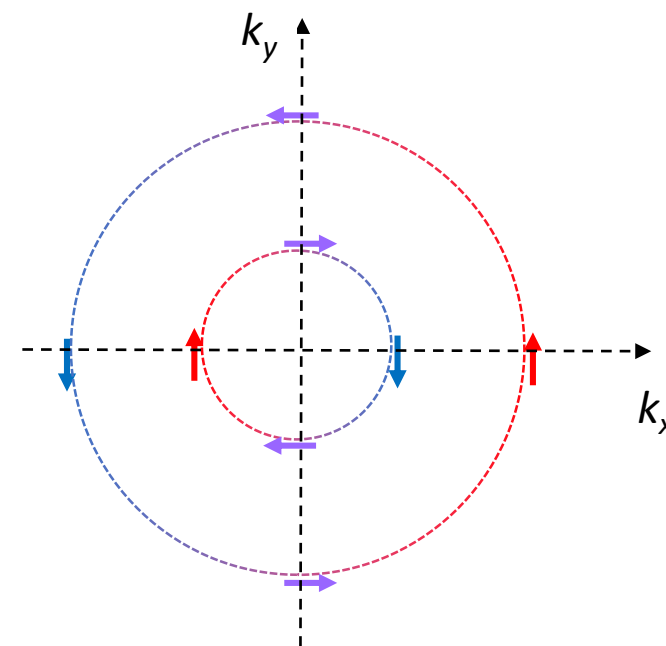
Chiral spin texture characterized by $k_x \sigma_y$ ($k_y \sigma_x$) spin-momentum locking

$$H_{RE} = 0$$

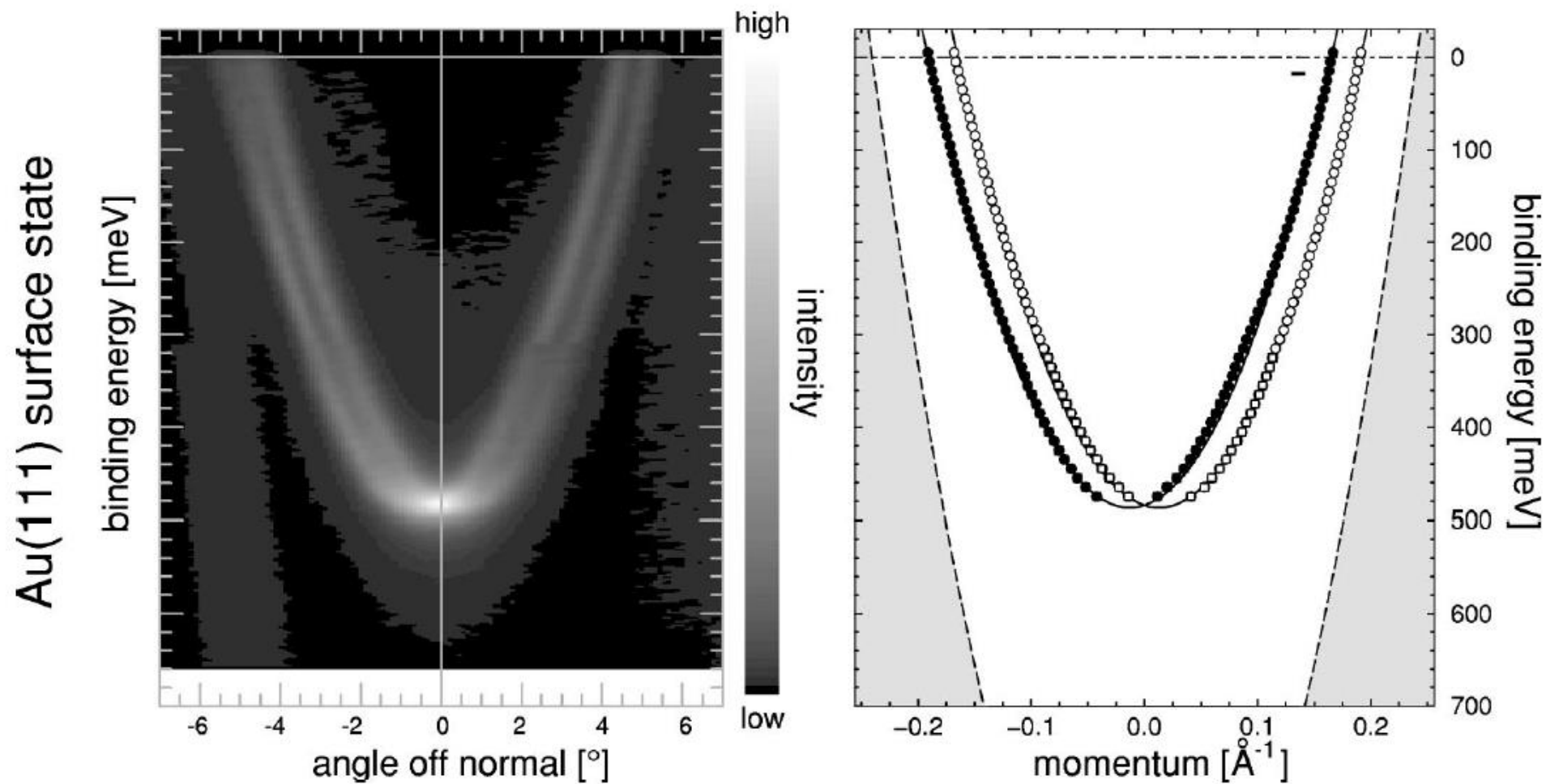


E_R is used to quantify the REE

Top view

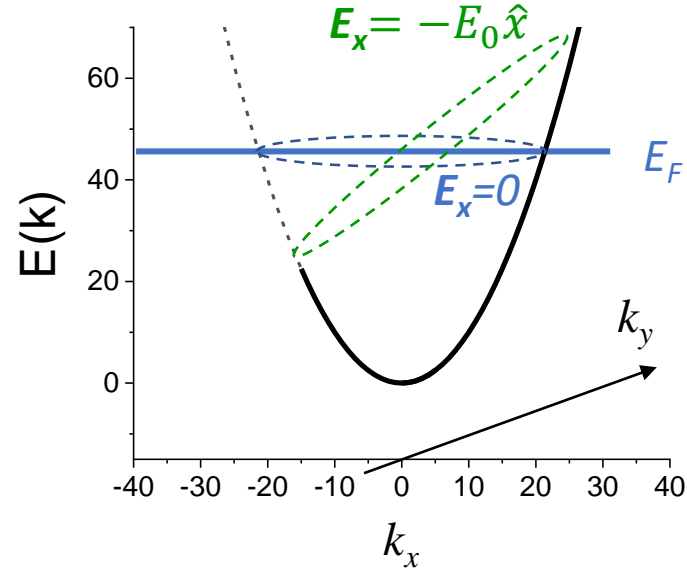


N.B.: arrow color code reflects the σ_y character

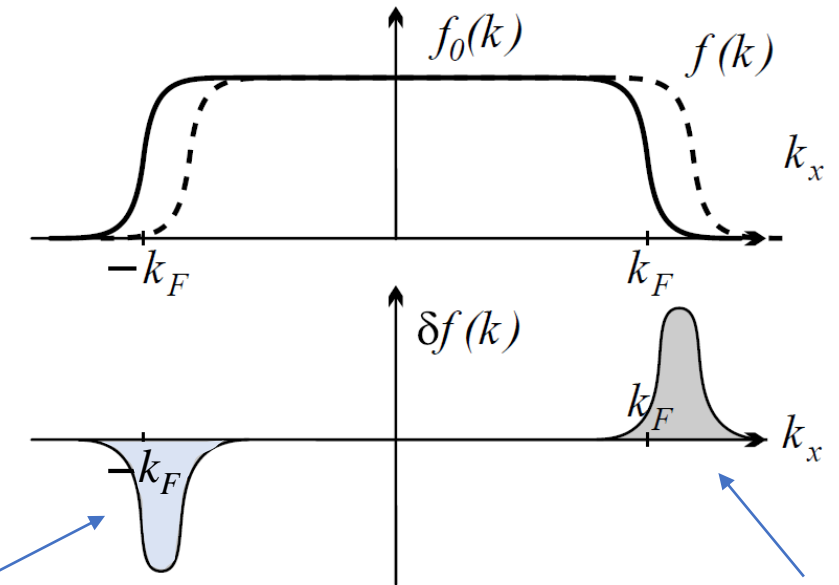
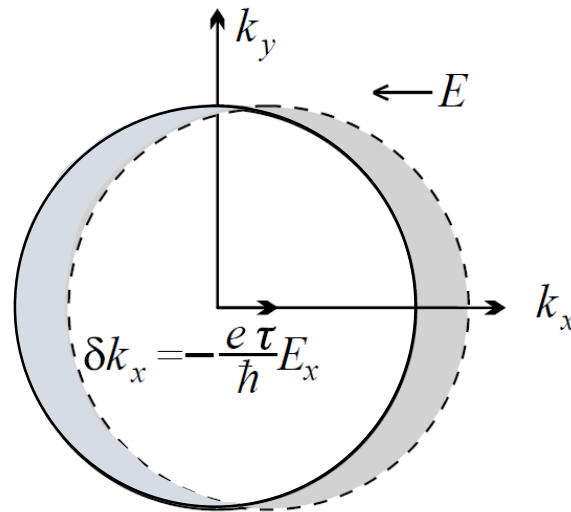




Band dispersion



Momentum space



Emptied states

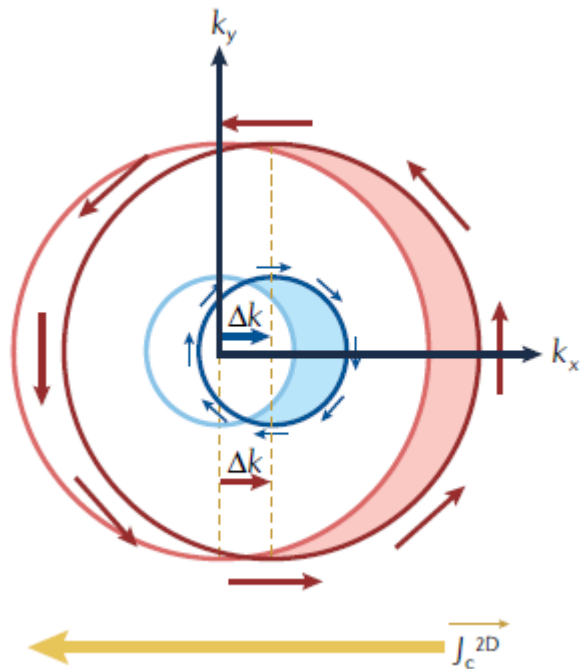
Extra filled states

Displacement of the Fermi surface under the effect of an electric field generating an unbalanced distribution of states in the k -space:
increased (decreased) number of states with positive (negative) k_x moment



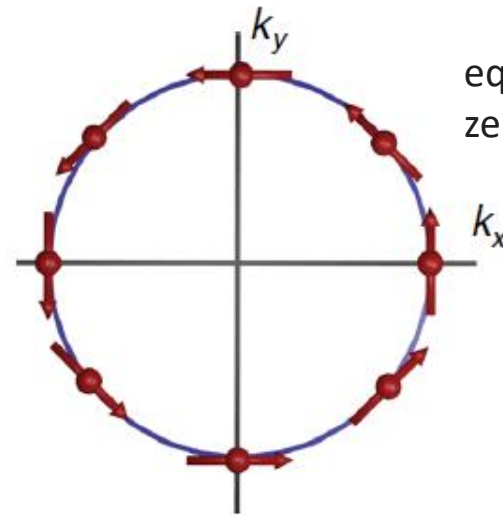
Rashba spin texture for the majority chiral states
The reversed chirality will give an opposite but lower contribution

Displacement of the Fermi surface
under the effect of an electric field

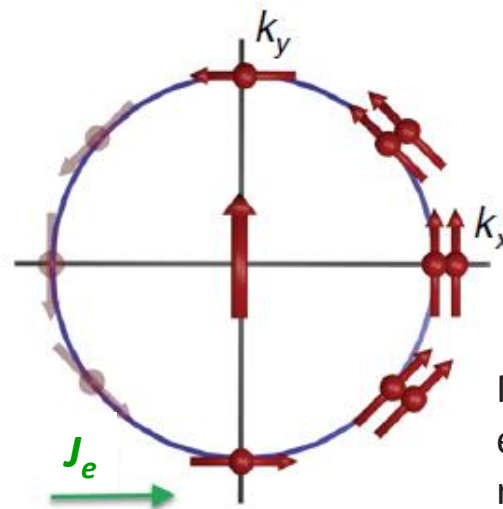


Current flows opposite to electrons

$$J_c = -J_e$$



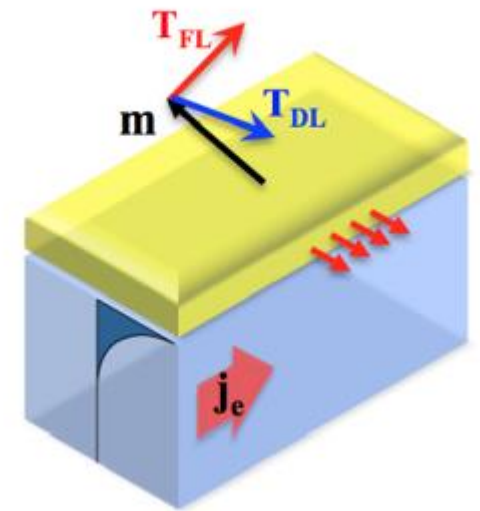
equilibrium ($J_e = 0$) with
zero net spin density



Nonequilibrium redistribution of
eigenstates in an applied electric field
resulting in a nonzero spin density



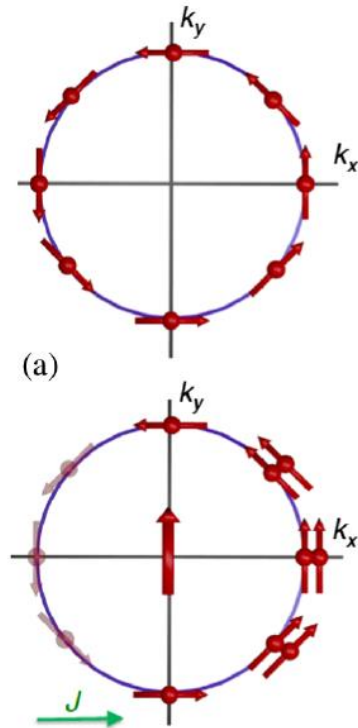
REE - SOT



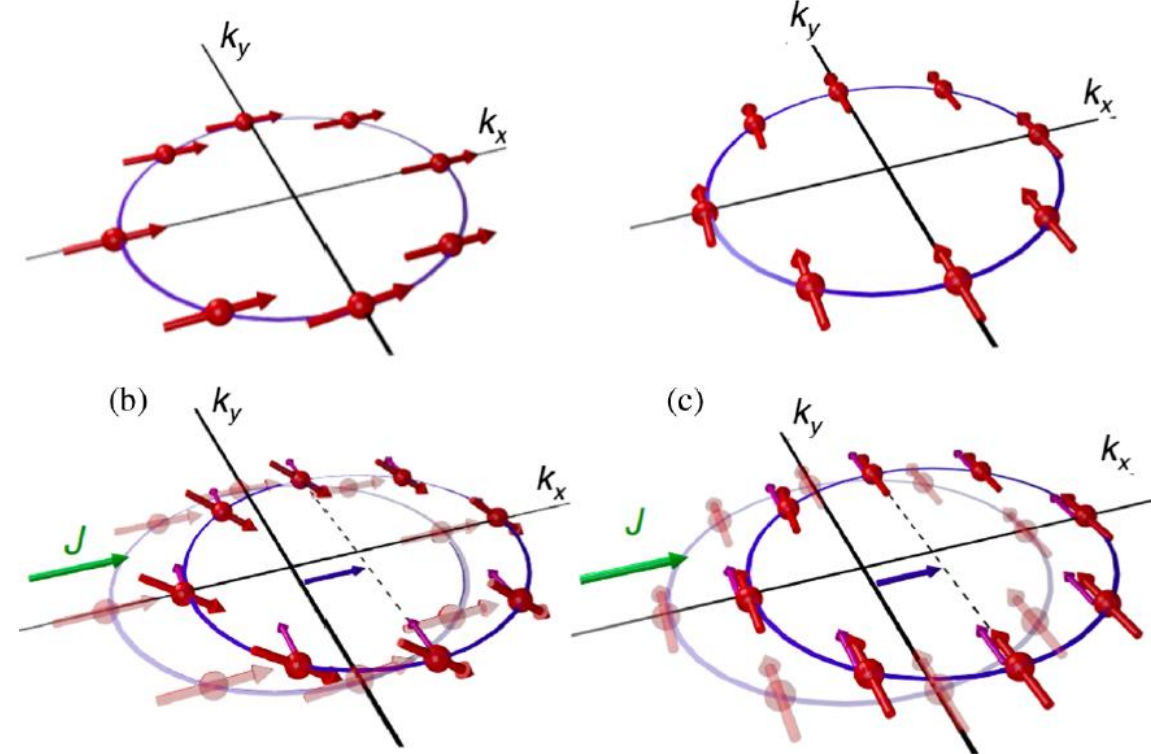
Torque on the top magnetic
layer via exchange



Non magnetic material



Ferromagnetic material



(a) Top: Rashba spin texture for one of the chiral states in equilibrium with zero net spin density. **Bottom:** Nonequilibrium redistribution of eigenstates in an applied electric field resulting in a nonzero spin density due to broken inversion symmetry of the spin texture. The exchange coupling of the carrier spin density to magnetization overlayer is responsible for the REE-SOT torque

(b) Top: A model equilibrium spin texture in a 2D Rashba spin-orbit coupled system with an additional time-reversal symmetry breaking exchange field (magnetization) of a strength much larger than the spin-orbit field. In equilibrium, all spins in this case align approximately with the x direction of the exchange field (magnetization). **Bottom:** In the presence of an electrical current along the x direction the Fermi surface (circle) is displaced along the same direction. When moving in momentum space, electrons experience an additional spin-orbit field proportional to $\hat{z} \wedge \mathbf{p}_x$ (purple arrows). In reaction to this nonequilibrium current-induced field ($\frac{d\mathbf{m}}{dt} = -\gamma(\mathbf{m} \wedge \mathbf{H}_{eff})$), spins tilt and generate a uniform, nonequilibrium out-of-plane spin density (REE-SOT torque).

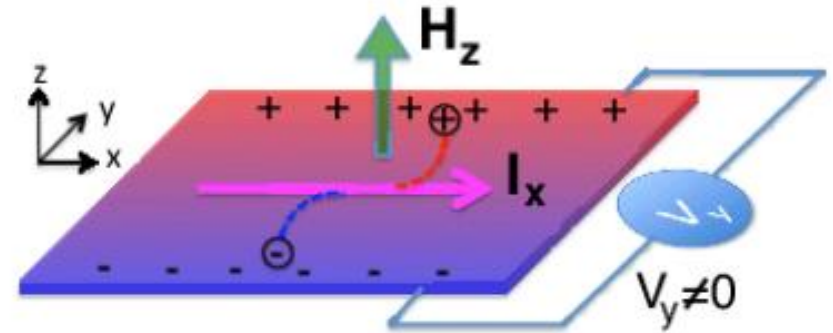
(c) Top: Same as in (b) for the y direction of the exchange field. **Bottom:** Same as in (b) but now with the current-induced spin-orbit field align with the exchange field, resulting in zero tilt of the carrier spins



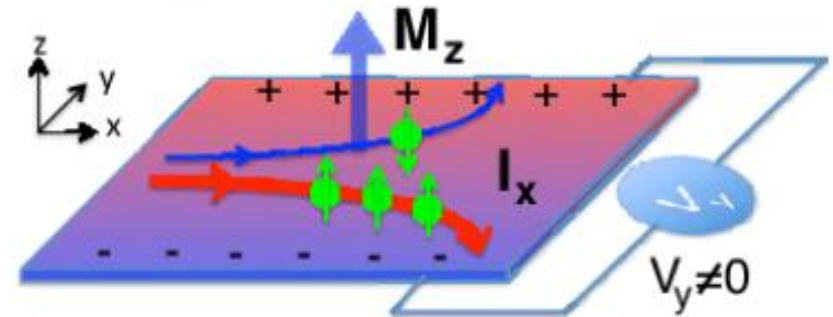
Hall effect (HE): The longitudinal current I_x under vertical external magnetic field H_z contributes to the transversal voltage V_y due to the Lorentz force experienced by carriers.

Anomalous Hall effect (AHE): The electrons with majority and minority spin (due to spontaneous magnetization M_z) have opposite "anomalous velocity" due to spin-orbit coupling. The spin polarization of the current causes unbalanced electron concentration at two transversal sides and leads to finite voltage V_y .

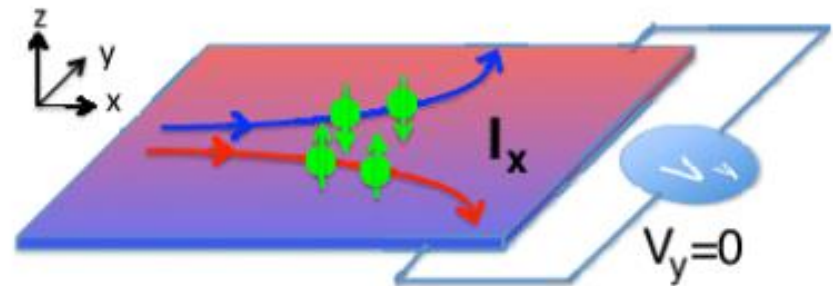
Spin Hall effect (SHE): In nonmagnetic conductor, equivalent currents in both spin channels with opposite velocity leads to a net spin current in transversal direction (but with balanced electron concentration at both sides $\Rightarrow V_y = 0$)



(a) Hall effect



(c) Anomalous Hall effect

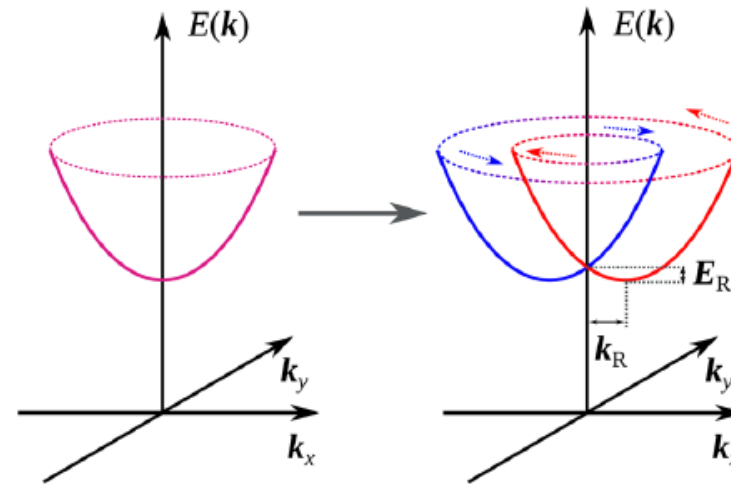


(e) Spin Hall effect

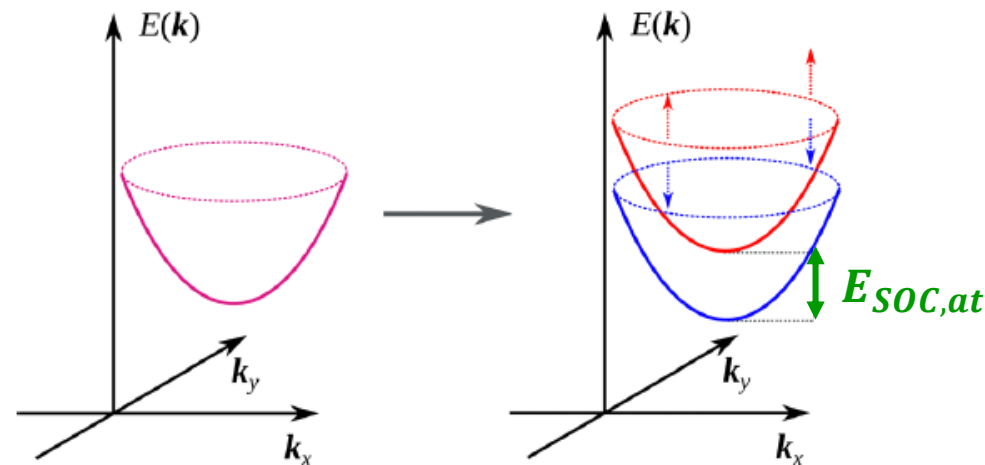


REE SOC: acts only on in-plane spins

$$E_R = \alpha_R (\hat{\mathbf{z}} \wedge \mathbf{p}_{//}) \cdot \boldsymbol{\sigma}_{//}$$



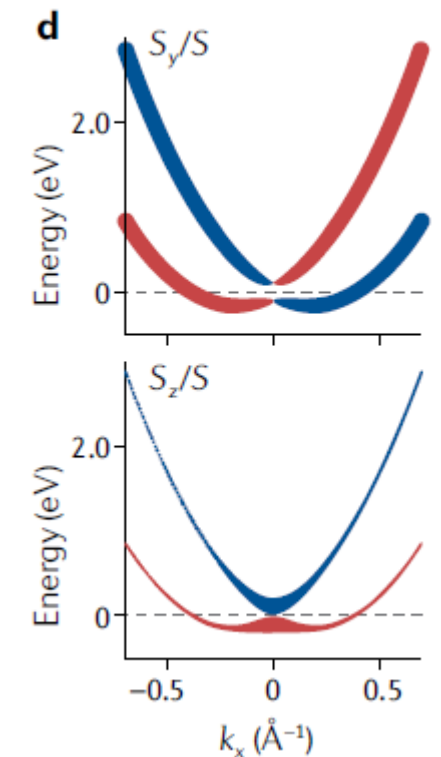
REE + atomic
SOC



Atomic SOC: acts on both in-plane
and out-of-plane spins

$$\begin{aligned} E_{SOC,at} &= \frac{e\hbar}{2m_e^2c^2} (\nabla V_{at} \wedge \mathbf{p}) \cdot \boldsymbol{\sigma} = \\ &= \mathbf{B}_{SOC,at} \cdot \boldsymbol{\sigma} \propto V_{SO} \mathbf{l} \cdot \boldsymbol{\sigma} \end{aligned}$$

Magnetization along z



normalized S_x (S_y) components as
line thickness (different
orientations are in red and blue).
Reduced momentum locking for
 $k \approx 0 \Rightarrow$ stronger S_z character



Spin split bands due to REE + Atomic SOC

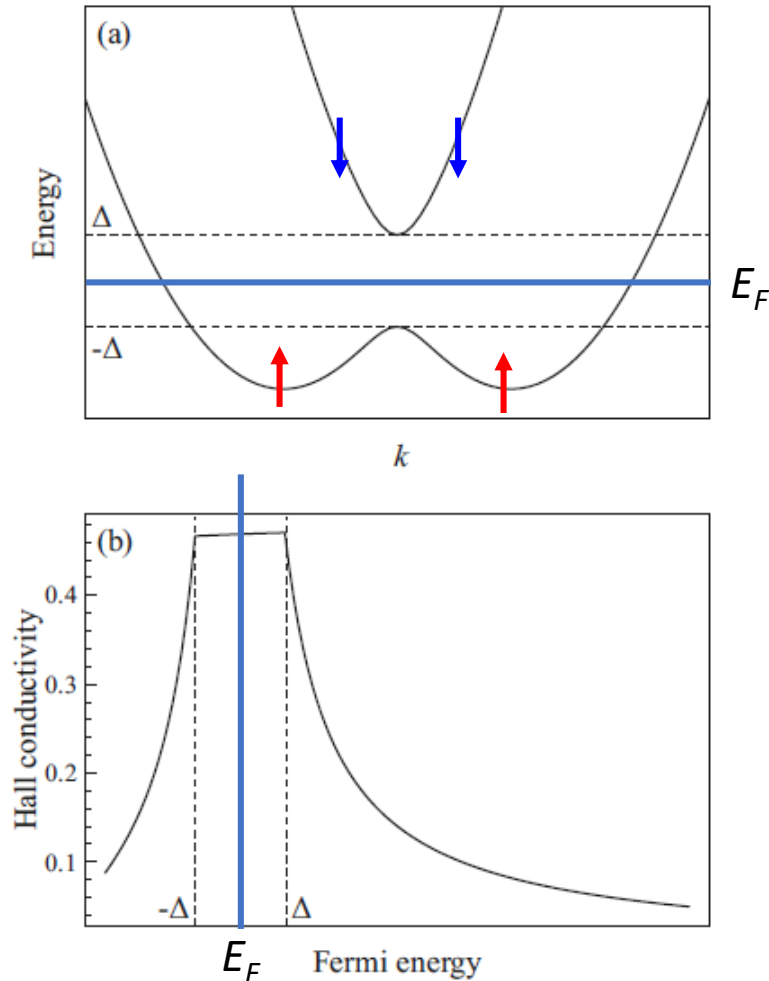


FIG. 6. Anomalous Hall effect in a simple two-band model. (a) Energy dispersion of spin-split bands. (b) The Hall conductivity $-\sigma_{xy}$ in the units of e^2/h as a function of Fermi energy.

If $E_F < -\Delta$, the states with energies just below $-\Delta$, which contribute most to the AHE, are empty.

If $E_F > \Delta$, contributions from upper and lower bands cancel each other, and the AHE decreases quickly as E_F moves away from the band gap.

If E_F is in the gap region $-\Delta < E_F < \Delta$, the AHE is resonantly enhanced and reaches its maximum value about $-e^2/2h$.

Similar arguments hold for the spin-split polarized bands of a bulk material



Skew (Mott) scattering: inhomogeneous atomic potential results in a inhomogeneous effective magnetic field

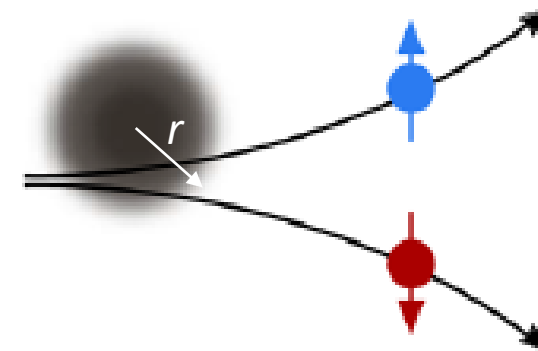
Atomic potential: $V(r) = \frac{Ze}{4\pi\epsilon_0 r}$

$$\nabla V = \frac{1}{r} \frac{dV(r)}{dr} \mathbf{r}$$

$$\mathbf{B}_{eff} = \frac{1}{mc^2} \nabla V \times \mathbf{p}$$

\mathbf{B}_{eff} is a function of $r \Rightarrow$ gradient of \mathbf{B}

Similar to Stern-Gerlach experiment:
opposite spins are deflected in opposite directions



Screw defects or impurities are the source of these extrinsic scattering events

AHE: unbalanced number of spin up and down \Rightarrow

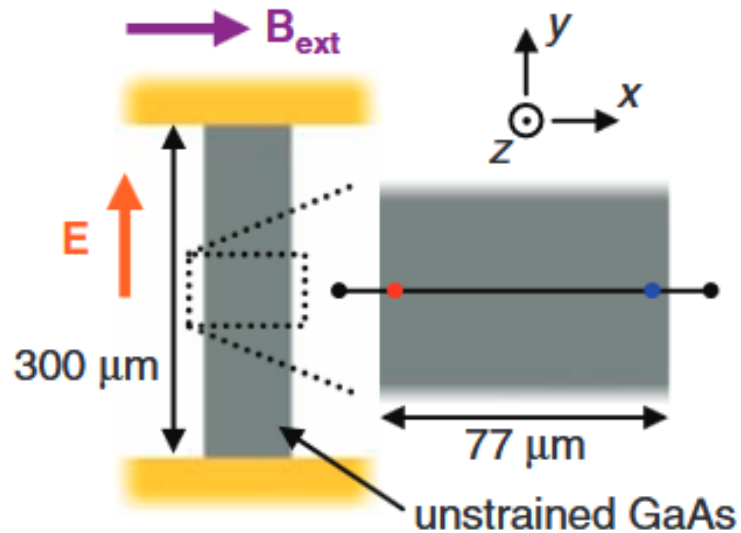
$$J_s \neq 0 \quad V_y \neq 0$$

SHE: balanced number of spin up and down \Rightarrow

$$J_s \neq 0 \quad V_y = 0$$



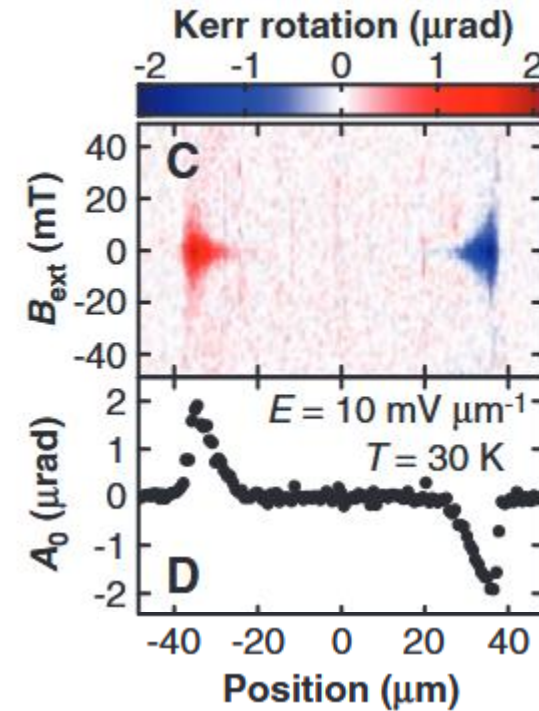
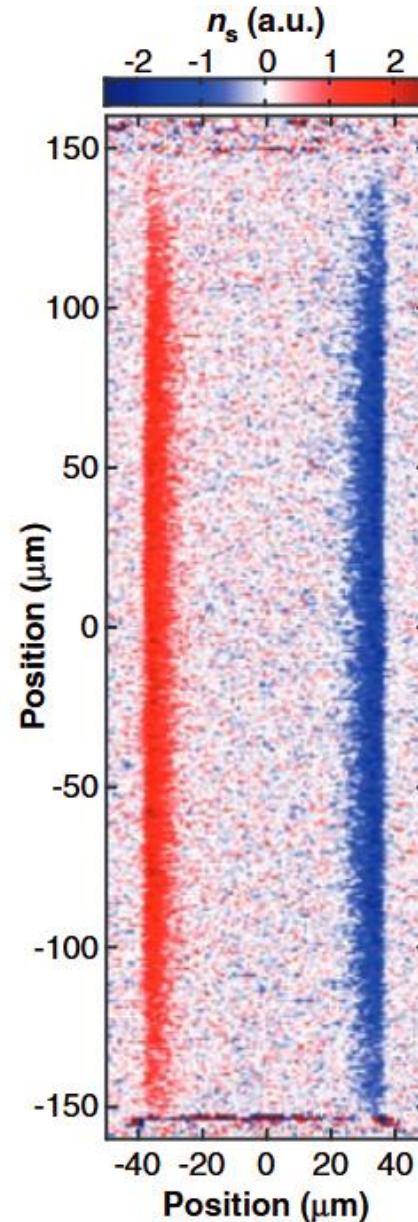
Observation of SHE by magneto-optical Kerr effect



2 μm thick GaAs
 n_s is the spin density
 $T = 30\text{ K}$ and $E = 10\text{ mV}/\mu\text{m}$

$$J_s \cong 10\text{ nA}/\mu\text{m}^2$$

$$J_c \cong 50\text{ }\mu\text{A}/\mu\text{m}^2$$

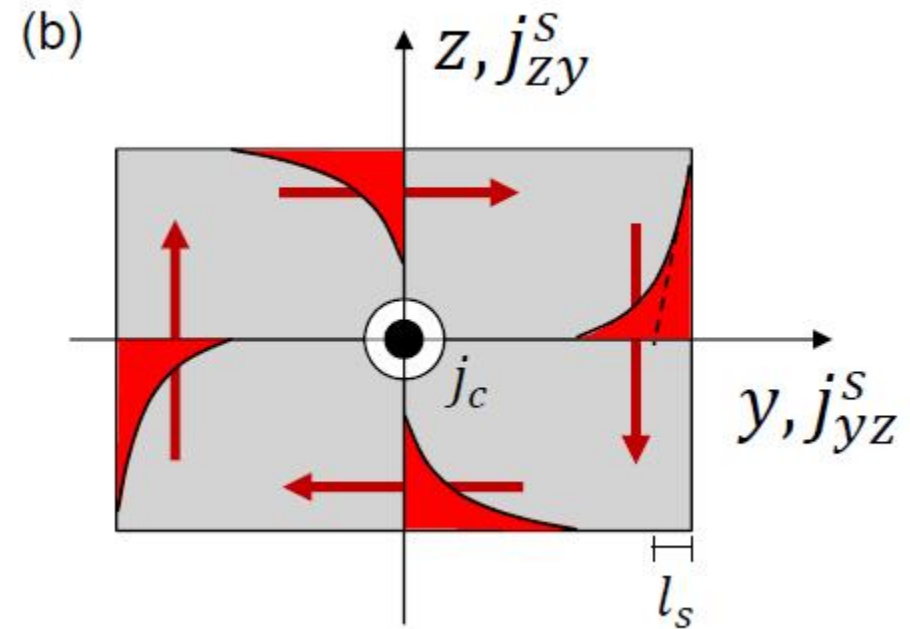
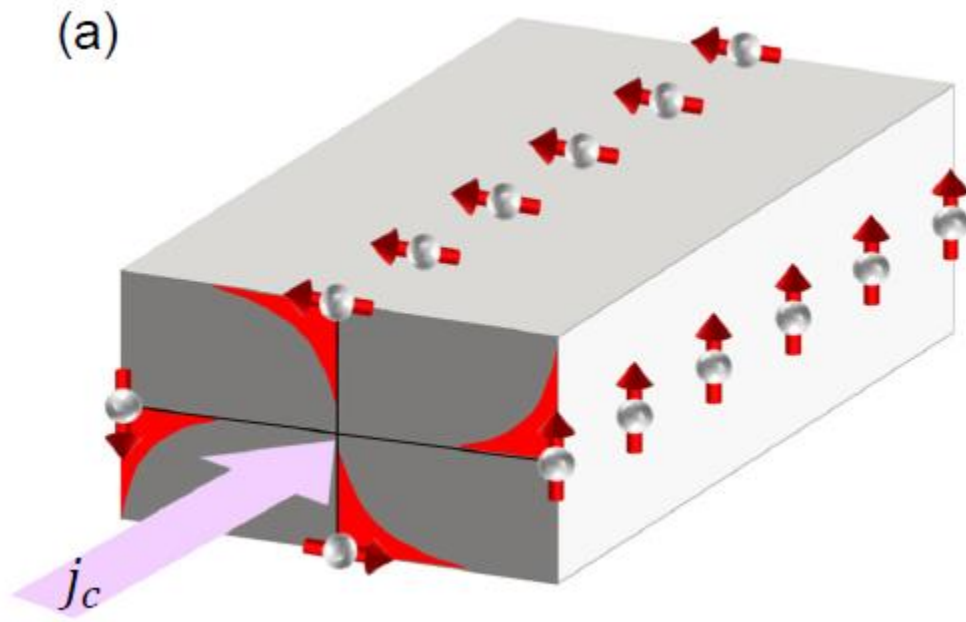


Out-of-plane
spin polarization

$$P_x = P_y = 0 \quad P_z(y) = P_z(0)e^{-y/L_s}$$

$$P_z(0) = -\frac{\gamma \mu n_s E L_s}{D}$$

γ coefficient accounting for the SOC
 μ and D are the mobility and the diffusion coefficient
 $L_s = \sqrt{D\tau_s}$ is the spin diffusion length $\cong 10\text{ }\mu\text{m}$
 τ_s is the spin lifetime



Charge current: $J_c = J^+ + J^-$

$$J_s = \theta_{SH} \frac{\hbar}{2e} J_c \wedge \sigma$$

Spin current: $J_s = \frac{\hbar}{2e} (J^+ - J^-)$

$\theta_{SH}(Pt, Ta) \approx 0.05 - 0.2$
spin to charge conversion factor



SOC has opposite effect
in Pt vs Ta

Pt: more than half filled
Ta: less than half filled

3 Sc Scandium 44.96	4 Ti Titanium 47.88	5 V Vanadium 50.94	6 Cr Chromium 52.00	7 Mn Manganese 54.94	8 Fe Iron 55.85	9 Co Cobalt 58.93	10 Ni Nickel 58.69	11 Cu Copper 63.55	12 Zn Zinc 65.39
21 Y Yttrium 88.91	22 Zr Zirconium 91.22	23 Nb Niobium 92.91	24 Mo Molybdenum 95.94	25 Tc Technetium 98	26 Ru Ruthenium 101.1	27 Rh Rhodium 102.9	28 Pd Palladium 106.4	29 Ag Silver 107.9	30 Cd Cadmium 112.4
57-71 La-Lu Lanthanides	72 Hf Hafnium 178.5	73 Ta Tantalum 180.9	74 W Tungsten 183.8	75 Re Rhenium 186.2	76 Os Osmium 190.2	77 Ir Iridium 192.2	78 Pt Platinum 195.1	79 Au Gold 197.0	80 Hg Mercury 200.6
89-103 Ac-Lr Actinides	104 Rf Rutherfordium 261	105 Db Dubnium 262	106 Sg Seaborgium 266	107 Bh Bohrium 264	108 Hs Hassium 277	109 Mt Meitnerium 268	110 Ds Darmstadtium 271	111 Rg Roentgenium 272	112 Cn Copernicium 285

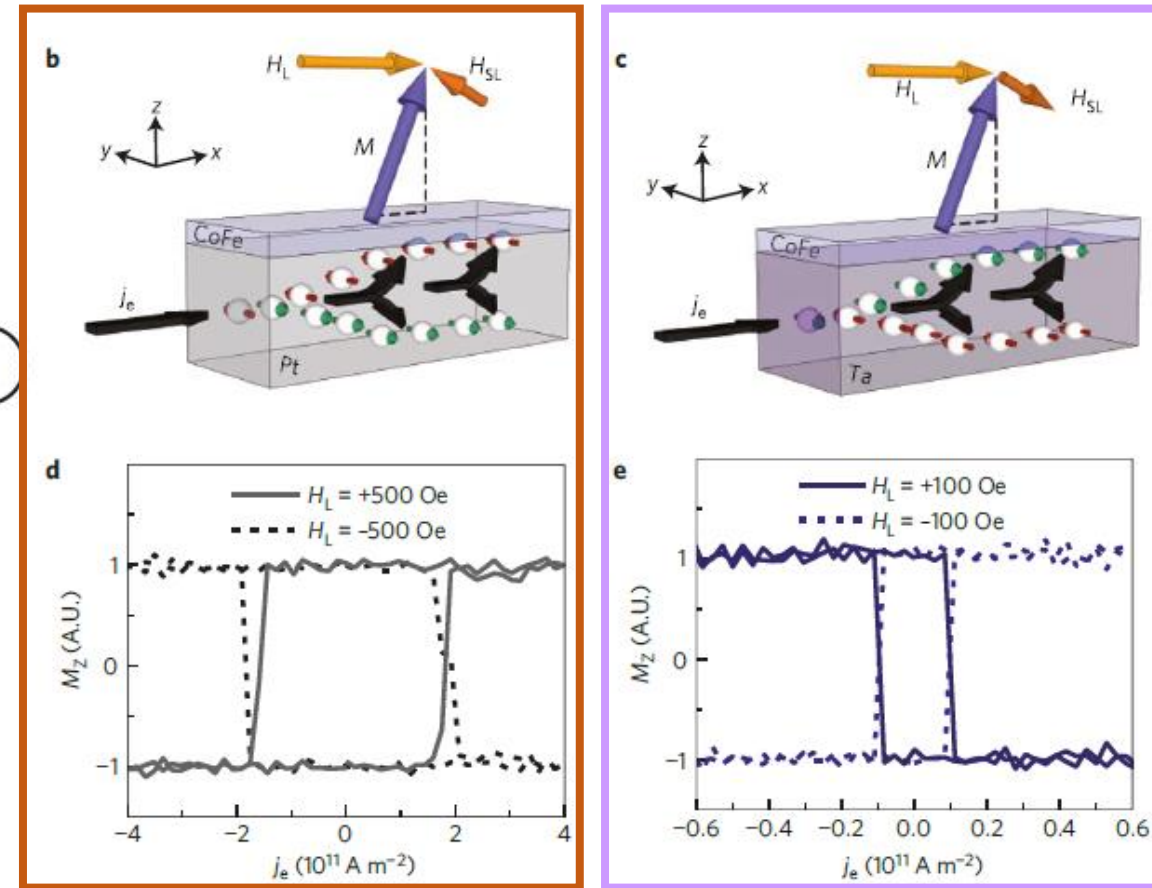
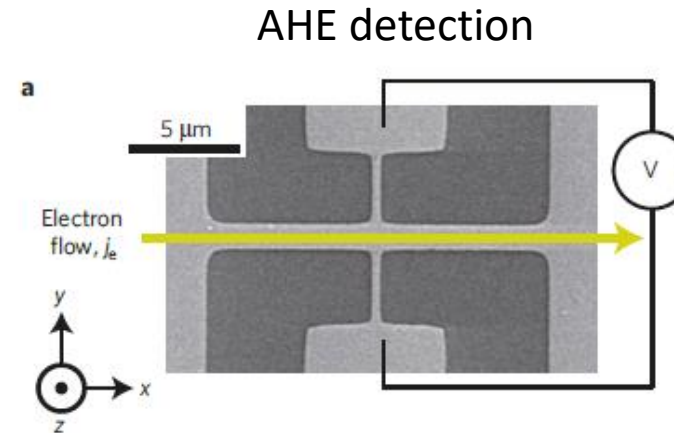
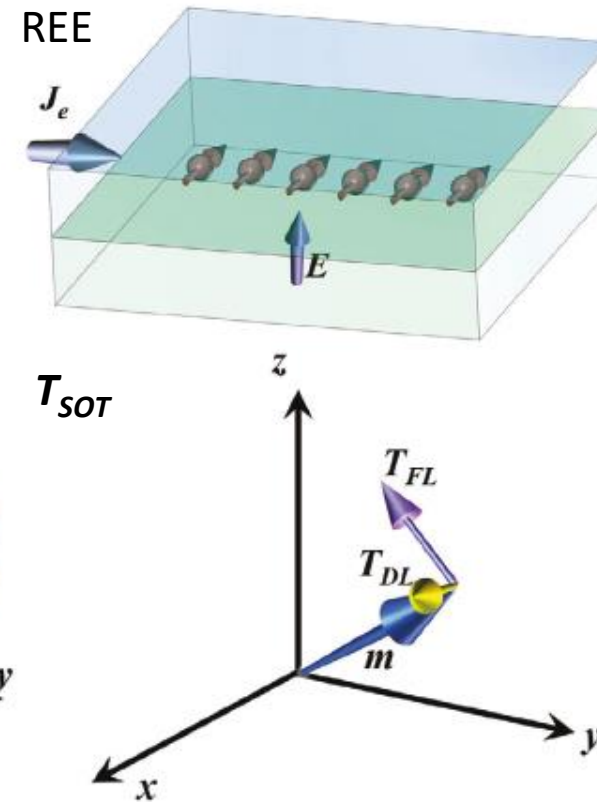
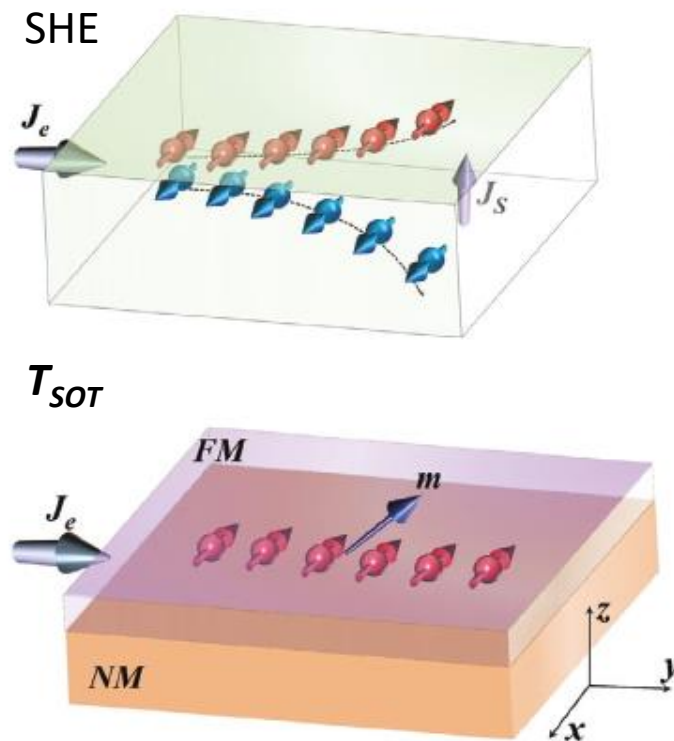


Figure 2 | Current-induced switching under a constant in-plane longitudinal field. **a**, Scanning electron micrograph of a Hall cross. **b,c**, Illustrations of Pt/CoFe/MgO (**b**) and Ta/CoFe/MgO (**c**) in the up magnetization state with the injected electron current and applied longitudinal field H_L in the $+x$ direction. Owing to the combination of the current-induced Slonczewski-like torque (producing an effective field H_{SL}) and the applied longitudinal field, up magnetization is stable in Pt/CoFe/MgO whereas it is unstable in Ta/CoFe/MgO. **d,e**, Out-of-plane magnetization M_z (normalized anomalous Hall signal) as a function of electron current density j_e under a constant H_L in Pt/CoFe/MgO (**d**) and Ta/CoFe/MgO (**e**). The magnitude of H_L is 500 Oe for Pt/CoFe/MgO (**d**) and 100 Oe for Ta/CoFe/MgO (**e**). When H_L is reversed from $+x$ (solid line) to $-x$ (dotted line), the stable magnetization direction under a given current polarity reverses.

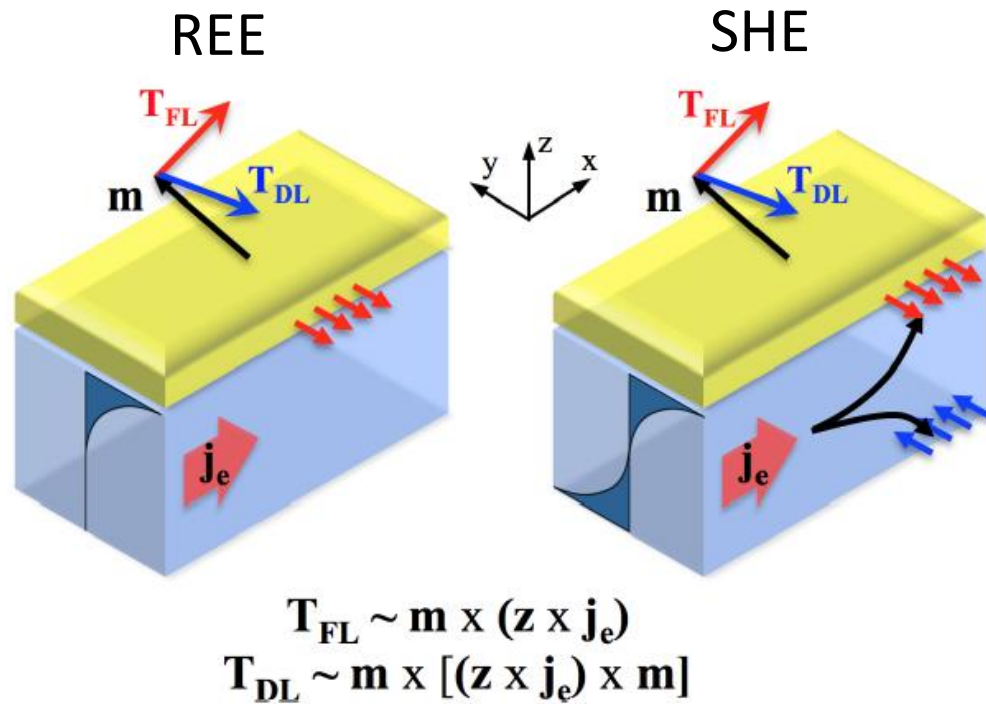


SHE: a charge current flowing in an NM layer generates a spin current owing to asymmetric spin deflection induced by SOC. The polarization direction is perpendicular to both the directions of the charge and spin currents.

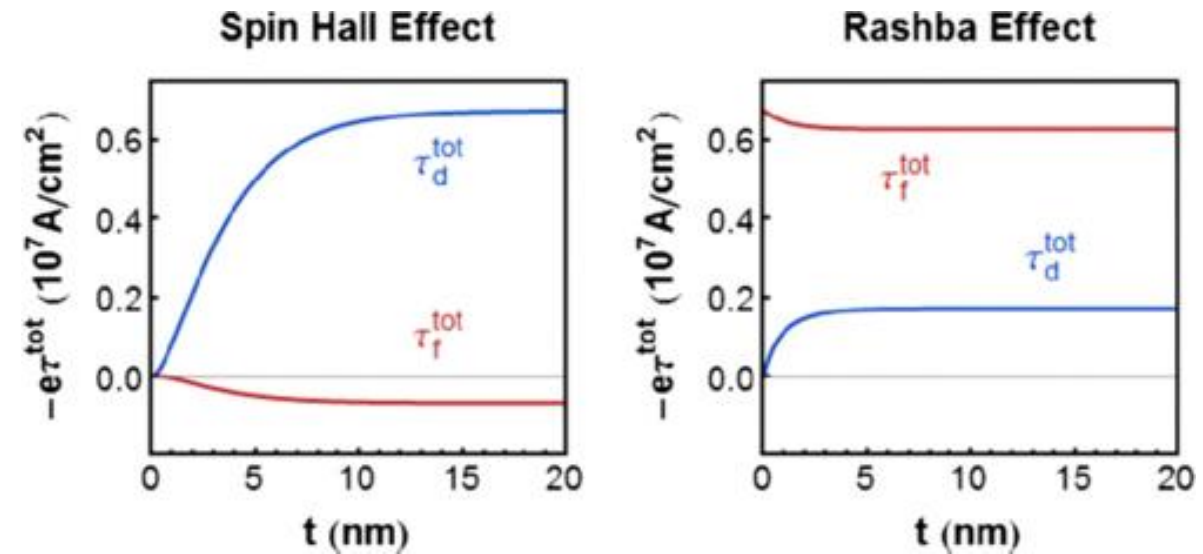


REE: an internal electrical field $\mathbf{E} = E_z \mathbf{z}$ is generated at the interface/surface because of the spatial inversion symmetry breaking. When an in-plane charge current flows through the FM/NM heterostructure, the conduction electrons near the interface move in the electrical field \mathbf{E} , and they experience an effective magnetic field perpendicular to the current direction (SOC-induced Rashba field \mathbf{H}_{RE}): accumulation of spins perpendicular to both the charge current \mathbf{J}_e and $\mathbf{E} = E_z \mathbf{z}$.

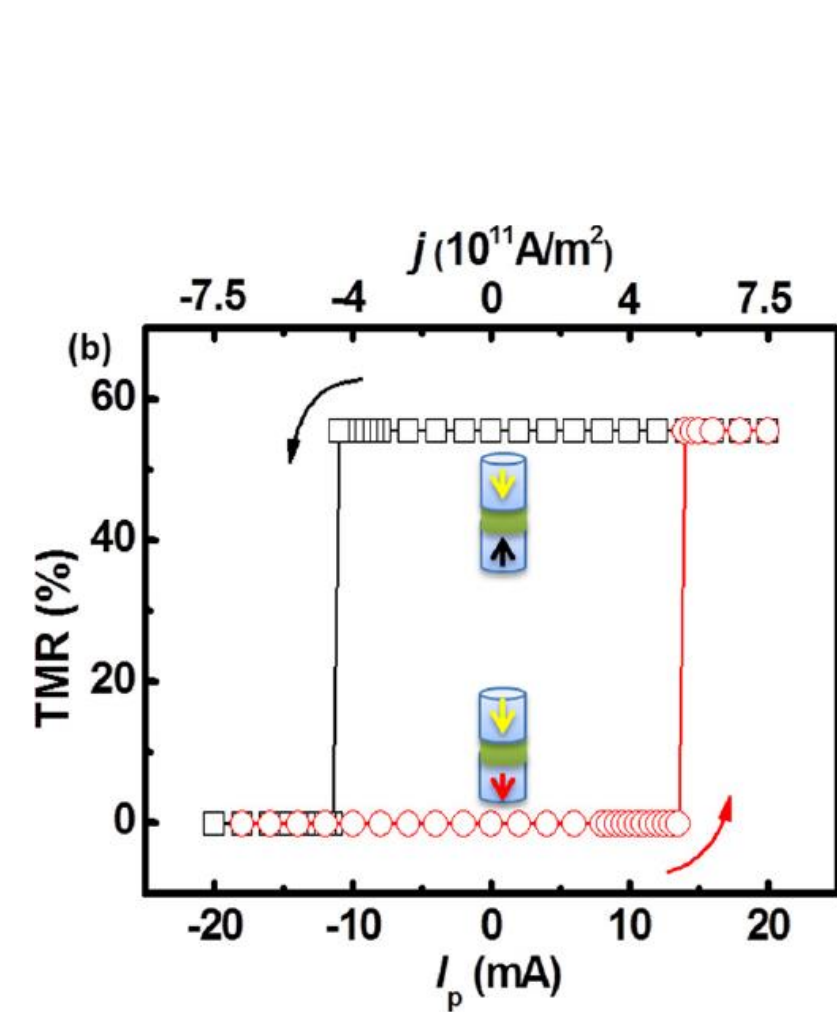
As the spin current diffuses into the adjacent FM layer, a SOT torque \mathbf{T}_{SOT} (via exchange) is exerted on the magnetization \mathbf{m} . This torque has two components $\mathbf{T}_{\text{SOT}} = \mathbf{T}_{\text{DL}} + \mathbf{T}_{\text{FL}}$



Both mechanisms produce damping-like and field-like torques. The small red and blue arrows denote the nonequilibrium spin density accumulating at the interfaces, and their corresponding spatial distribution is sketched as a shaded area on the structure's side. The large red and blue arrows represent the field-like and damping-like torques, respectively.



Torque components as a function of the nonmagnetic metal thickness



TMR as a function of current pulse amplitude I_p injected in the Ta electrode using 50 ns long pulses under an in-plane magnetic field $H = -0.4$ kOe along the current. The arrows show the sweep direction of I_p .

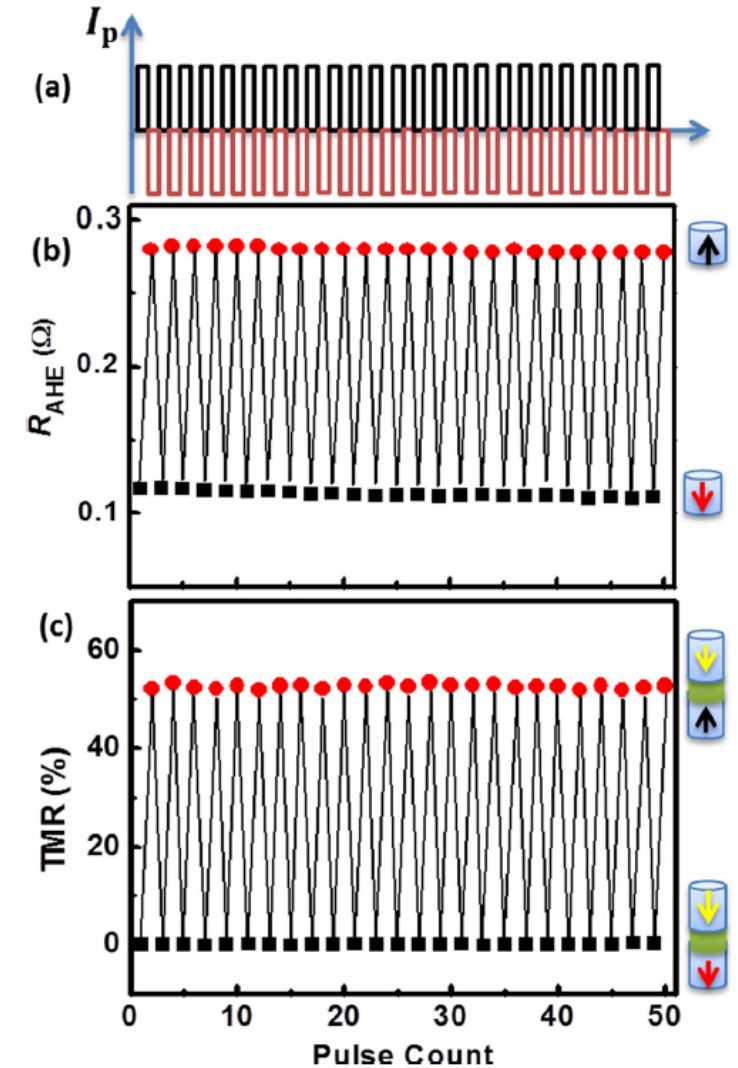
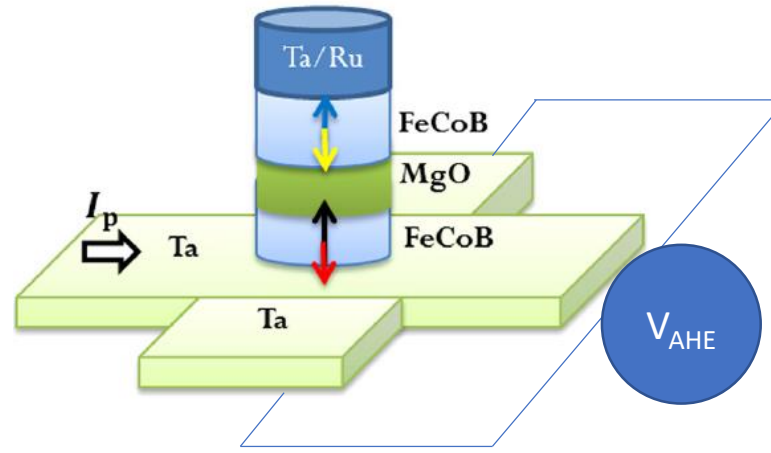
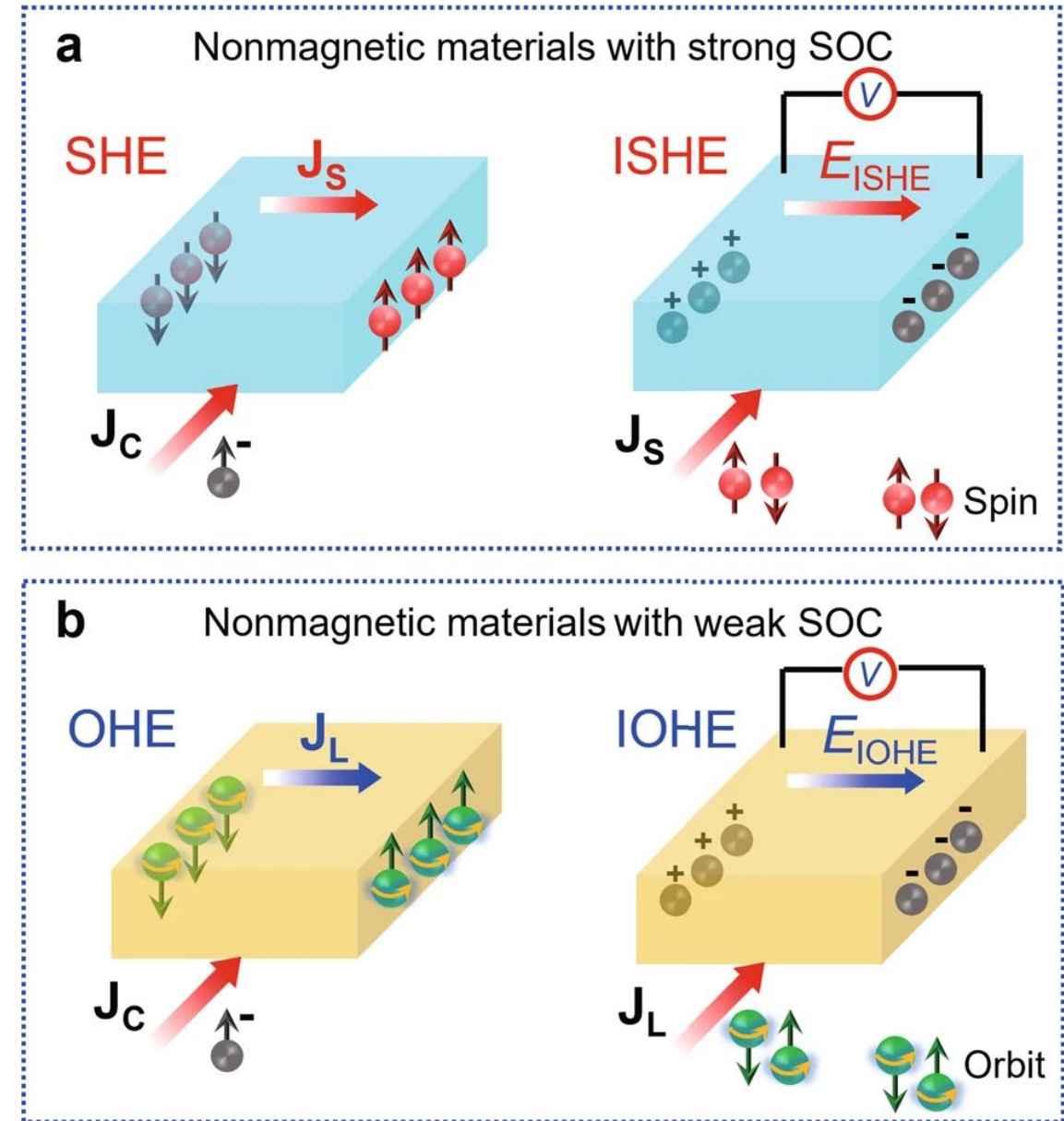


FIG. 3. (a) Schematic of the pulse sequence. (b) The AHE resistance (proportional to the M_z component of the bottom FeCoB layer) and (c) TMR measured after the injection of positive (black squares) and negative (red circles) current pulses of amplitude $I_p = 20$ mA and 50 ns long under $H_1 = -0.4$ kOe.



SHE and ISHE (invers SHE) refer to the conversions of $J_c \rightarrow J_s$ and $J_s \rightarrow J_c$ in the heavy metals with strong SOC, where a transverse flow of spin angular momentum and voltage are generated, respectively.

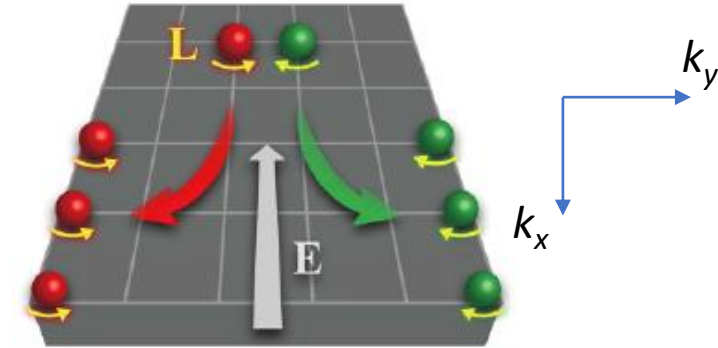


OHE and IOHE are the conversion of $J_c \rightarrow J_L$ and $J_L \rightarrow J_c$ in the materials with weak SOC, where a transverse flow of orbital angular momentum and voltage are induced, respectively. Thanks to SOC in an adjacent FM layer, the orbital current exerts a torque on the FM layer



Schematic illustration of the OHE without SOC

The angular momentum \mathbf{L} is defined from localized orbitals around the atom at each lattice. In the presence of an external electric field \mathbf{E} , electrons with opposite \mathbf{L} deflect in the clockwise (red arrow) or anticlockwise (green arrow) direction.



Formal approach (ex. for p -waves)

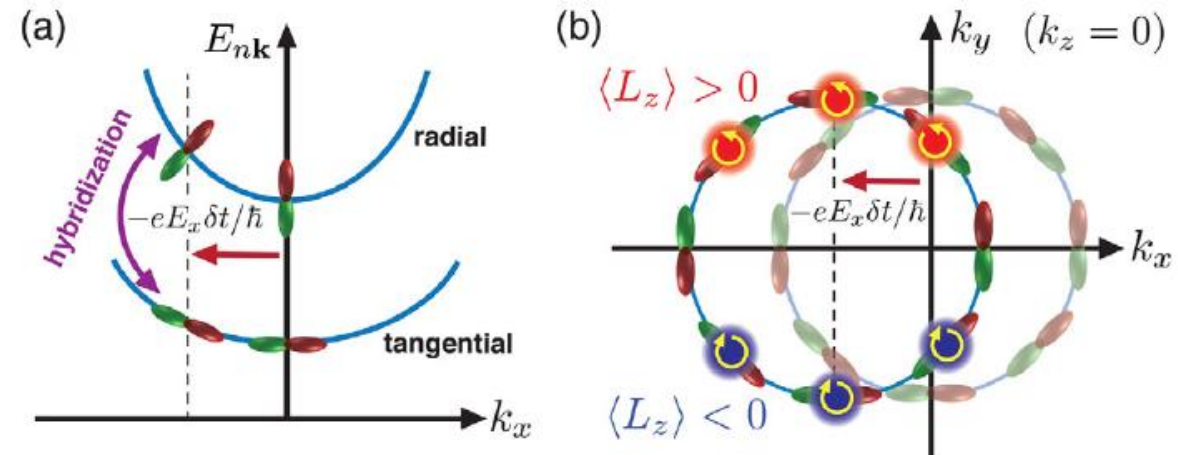
$$p_{radi} = \cos \phi p_x + \sin \phi p_y$$

$$p_{tang} = \sin \phi p_x - \cos \phi p_y$$

Under the effect of the external field, p_{radi} and p_{tang} get hybridized resulting in new states that can have finite L_z

Table 2. Matrix elements $\langle p_i | \hat{e} \cdot \mathbf{L} | p_j \rangle$.

	$\langle x $	$\langle y $	$\langle z $
$ x\rangle$	0	$i\hat{e}_z$	$-i\hat{e}_y$
$ y\rangle$	$-i\hat{e}_z$	0	$i\hat{e}_x$
$ z\rangle$	$i\hat{e}_y$	$-i\hat{e}_x$	0

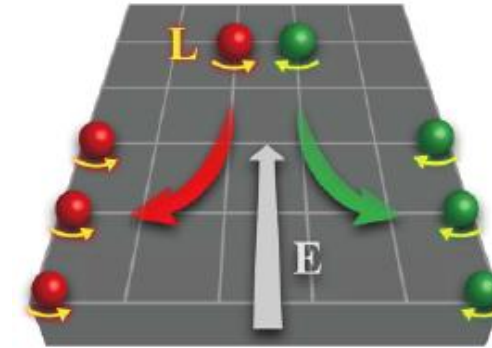


- (a) Schematic band structure with plots of wave function character at each band. Here, $k_y = k_z = 0$.
 (b) When an electron in the lower band is pushed from \mathbf{k} to $\mathbf{k} + \delta\mathbf{k}$ by an external electric field $\mathbf{E} = E_x \mathbf{x}$, positive (negative) L_z is induced for the nonequilibrium state with $k_y > 0$ ($k_y < 0$).



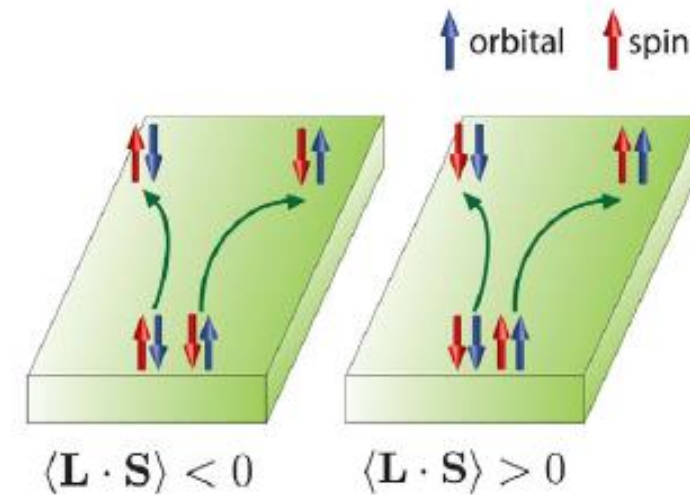
Schematic illustration of the OHE without SOC

The angular momentum \mathbf{L} is defined from localized orbitals around the atom at each lattice. In the presence of an external electric field \mathbf{E} , electrons with opposite \mathbf{L} deflect in the clockwise (red arrow) or anticlockwise (green arrow) direction.

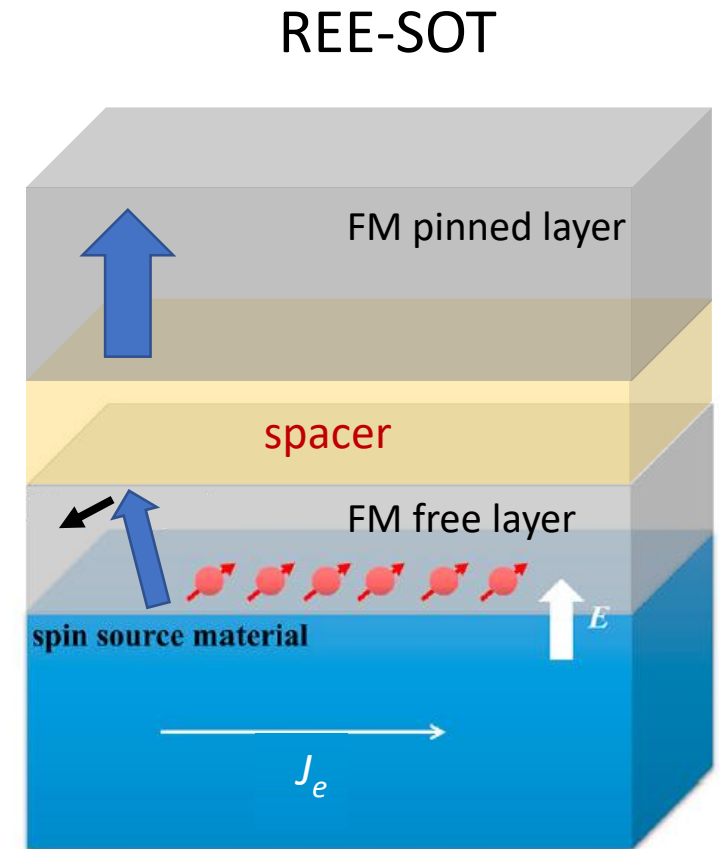
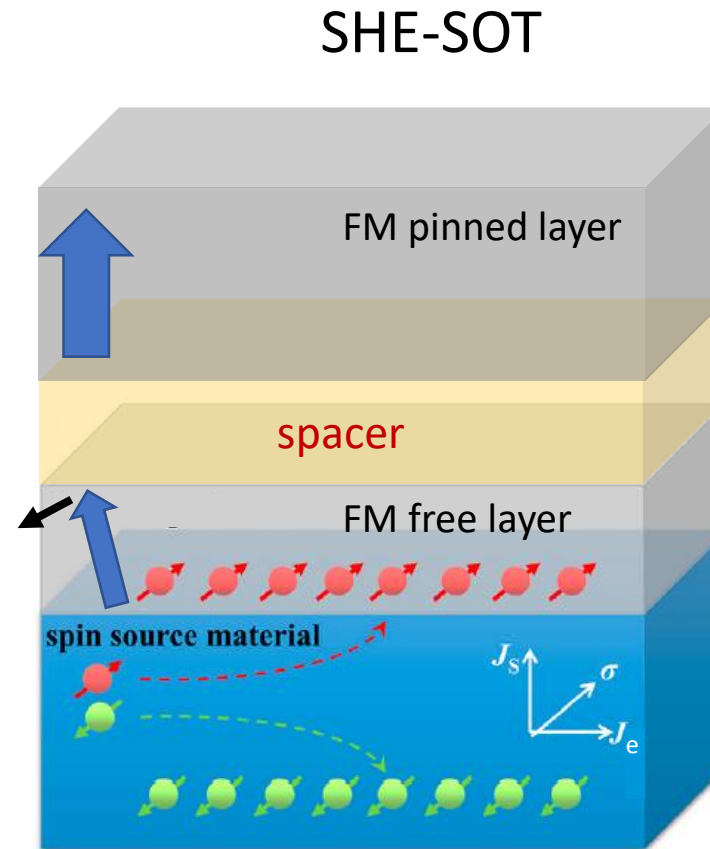
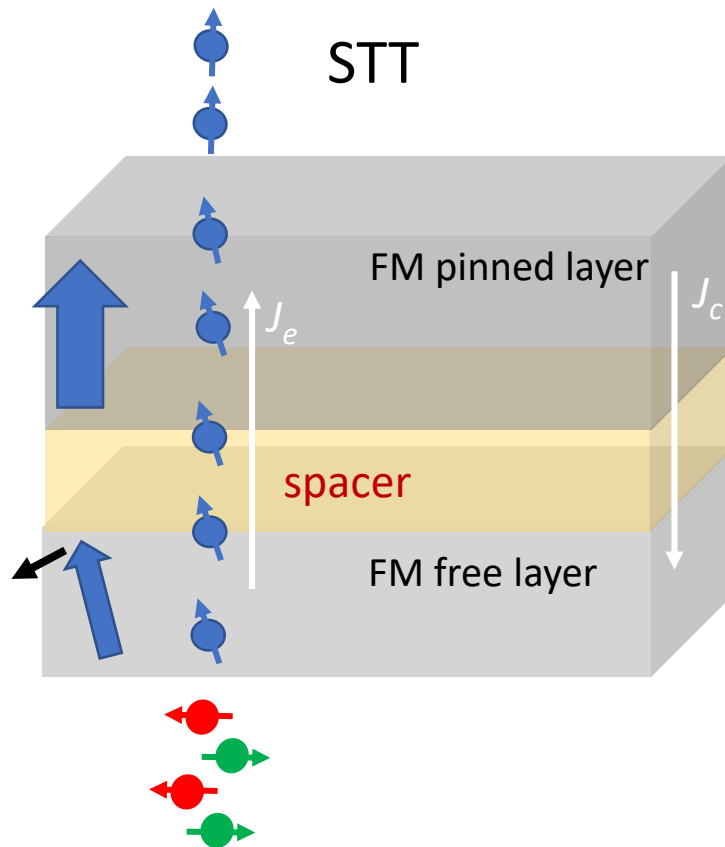


Schematic illustration when SOC is taken into account.

Spin and orbital momenta are locked by SOC. SHE occurs in the same or opposite direction of OHE depending on whether $\mathbf{L} \cdot \mathbf{S}$ is positive or negative.



The intrinsic SHE then emerges as a by-product of the OHE resulting from the orbital-to-spin conversion in materials with nonzero SOC



SOT employs in-plane current injection:

- 1) separates the reading and writing paths
- 2) Less power since current does not need to pass through the insulating spacer